MZU QUESTIONS BANK FOR DEPT. OF MATHEMATICS (GZRSC)

Subject : Mathematics Paper Name: Vector Calculus and Solid Geometry Paper No. : MATH/2/CC/II Semester : II

Part A: Tick (v) the correct answer in the brackets provided:

- 1. If a*(b*c)=(a*b)*c for all $a,b,c \in A$, then the binary operation is said to be
 - (a) commutative((b) associative((c) distributive((d) none of the above(
- 2. The number of commutative binary operation on a finite set A having *n* elements is

(a)	2 ^{<i>n</i>}	()
(b)	n^{n^2}	()
(c)	$\frac{1+n^2}{2}$	()
(d)	$\frac{n^2 + n}{2}$	()

3. The number of binary compositions on a finite set A having *n* elements is

(a)	2^n	()
(b)	n^{n^2}	()
(c)	$\frac{1+n^2}{2}$	()
(d)	$\frac{n^2 + n}{2}$	()

4. The number of generators of a cyclic group of order 16 is

(a) 2	()
(b) 4	()
(c) 8	()
(d) 16	()
	1	c

5. If H and K be two subgroups of a group G such that H has 7 elements and K has 13 elements, then the number of elements of $H \cap K$ is

(a) 1	()
(b) 6	()

(c) 7 ()

(d) 20 ()

6. When 99²⁰ is divided by 25, the remainder is

(a) 20	()
(b) 1	()
(c) 15	()
(d) 5	()

7. What is the remainder if 8¹⁰³ is divided by 103?

(a) 2	()
(b) 4	()
(c) 16	()
(d) 8	()

8. A homomorphism of a group into itself is called

- (a) An isomorphism ()
- (b) An endomorphism ()
- (c) An automorphism ()
- (d) None of the above ()

9. On dividing 11⁷ by 18, the remainder is

(a)	12	()
(b)	13	()
(c)	11	()
(d)	18	()

10. If f is a homomorphism of G into G', then the set K of all those elements of G which are mapped by f onto the identity element of G' is called

(a) kernel of the homomorphism f ()

(b)	homomorphism f			()			
(c)	kernel of the isomorp	ohism f		()			
(d)	Isomorphism f			()			
11. If f(x)) is divided by (ax-b), then	the rem	ainder i	is			
a)	f(-b/a)			()			
b)	f(b/a)			()			
c)	f(a)			()			
d)	f(a)			()			
12. The v	alue of k such that	$4x^3-3x^2$	$^2+2x+k$ 1	nay be	divisible by (2	x+2) is		
a)	48			()			
b)	-48			()			
c)	24			()			
d)	-24			()			
13. If f(x) and $g(x)$ be two	polync	omials o	f degre	es m and n r	respectiv	vely, then $f(x).g(x)$ is	a
polyn	omial of degree							
a)	mn	()					
b)	m+n	()					
c)	m/n	()					
d)	m-n	()					
14. If x^{k+}	¹ is divided by x^{K-1} ,	the rem	nainder v	will be				
a)	positive	()					
b)	negative	()					
c)	0	()					
d)	Infinity	()					
15. When	$12x^4-5x^2-32x+6$ is c	livided	by x-3,	the rem	nainder is			
a)	0	()					
b)	27	()					
c)	-18	()					
d)	1	()					
16. If the	equation $x^3+2x^2+ax^3$	x+b=0	has one	of the	roots as comp	olex root	t c+id, then the real roo)t
is								
a)	2+2c	()					
b)	2-2c	()					
c)	-2+2c	()					
d)	-2-2c	()					
17. The e	quation $4x^3 - 13x^2 - 31$	1x+41=	=0 has					
a)	3 positive roots					()	
b)	only one positive r	oot wh	ich lies	betwee	n 0 and 1	()	
c)	No positive root					()	

d) only one positive root which lies between 1 and 2 () 18. The range of values of k for which the equation $x^4+4x^3-8x^2+k=0$ has all real roots is a) 0 and 3 () b) 1 and 3 () c) 0 and 1 () d) 1 and 2 () 19. An equation of odd degree a) always has an imaginary root () b) always has a real root) (c) has only imaginary root () d) None of these 20. If the sum of two roots of the equation $x^3-5x^2-16x+p=0$ is zero, then the value of p is a) 0 () b) 16 () c) 80 () d) 20 () 21. By Cardan's method, the solution of $x^3-18x-35 = 0$ is a) $5.w.w^2$ () b) $5.w-2.w^2$) (c) $5, w-2, w^2-2$) (d) $5, w, w^2 - 2$ () 22. w (cube roots of unity) is equal to a) $(-1/2)+i\sqrt{3/2}$) (b) $(1/2)-i\sqrt{3/2}$ () c) $(1/2)+i\sqrt{3}/2$ () d) $(-1/2)-i\sqrt{3/2}$ () 23. Solution of $x^3+8=0$ is a) 2, 2w, $2w^2$ () b) $-2, -2w, -2w^2$ () c) $-2, 2w, 2w^2$ () d) $-2, -2w, 2w^2$ () 24. W(1+w) =a) 0) (b) 1 () c) -1 () d) 2 (25. The equation of third degree with real coefficient whose two roots are 2 and i is a) $x^3 - 2x^2 + x - 2 = 0$ () b) $x^3 - 2x^2 - x - 2 = 0$ ()

c) $x^3 - 8 = 0$ ()

d) $x^3 + 8 = 0$ ()

SECTION – B Fill in the blanks

1. If $a * b = b * a$ for all $a, b \in A$, then the binary operation * is said to be	
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2. The identity element of R with respect to multiplication is _____

3. Any two right(left) cosets of a subgroup are either disjoint or ______

4. Every group of ______ order is cyclic

5. The order of each subgroup of a finite group is a ______ of the order of the group.

6. If G is an infinite cyclic group, then G has exactly ______ generators.

- 7. If f(x) and g(x) are nonzero polynomials in F[x], then f(x)+g(x) is nonzero and $deg(f(x)+g(x)) = \dots$
- 8. A polynomial f(x) is completely divisible by (x-h) if and only if $f(h) = \dots$
- 9. If f(x) is divided by x+a, the remainder is
- 10. The equation $x^5+2x^4+2x^3+4x^2+x+2=0$ has multiple roots.
- 11. The equation $x^{12}-x^4+x^3-x^2+1=0$ has at least complex roots.
- 12. If α,β,γ are the roots of the equation $3x^3-4x^2+7=0$, then $(1/\alpha) + (1/\beta) + (1/\gamma)$ is
- 13. If $x^3 = a^3$, then $x = \dots$

14. By using De Moivre's theorem, cube roots of -1 are

15. The value of $(i)^{2/3}$ are

Answer Key

Part A

1. (b) 2. (d) 3. (a) 4. (c) 5. (a). 6. (c) 7. (d) 8. (c) 9. (c) 10. (a) 11. (b) 12. (a) 13. (b) 14. (c) 15. (b) 16. (d) 17. (d) 18. (a) 19. (b) 20. (c) 21. (c) 22. (a) 23. (b) 24. (c) 25. (a)

Part B

1. Commutative 2. 1 3. Identical 4. Prime 5. Divisor 6. Two 7. max $\{\deg(f(x)), \deg(g(x))\}$ 8. 0 9. f(-a) 10. two 11. six 12. 0 13. a, aw, aw² 14. -1, (1/2)+i\sqrt{3/2}, (-1/2)+i\sqrt{3/2} 15. Cos $\{(4k\pi + \pi)/3\}$ + iSin $\{(4k\pi + \pi)/3\}$ (k=0,1,2)

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Subject : Mathematics Paper Name: Vector Calculus and Solid Geometry Paper No. : MATH/4/CC/IV Semester : IV

Part A: Tick (v) the correct answer in the brackets provided:

- 1. Given the scalar field defined by $\phi(x, y, z) = 3x^2z xy^3 + 5$ at (1, -2, 2) is (a) 18 () (b) 19 () (c) 20 () (d) 21. () 2. When $\vec{a} = 3\hat{i} - \hat{j} - 4\hat{k}$, $\vec{b} = -2\hat{i} + 4\hat{j} - 3\hat{k}$ and $\hat{c} = \hat{i} + 2\hat{j} - \hat{k}$ then unit vector parallel to
- $2\vec{a}-\vec{b}+3\vec{c}$ is

(a)
$$11\hat{i} - 8\hat{j} - 4\hat{k}$$
 () (b) $\frac{11\hat{i} - 8\hat{j} - 4\hat{k}}{\sqrt{185}}$ ()
(c) $\frac{11\hat{i} - 8\hat{k}}{\sqrt{185}}$ () (d) $\frac{11\hat{i} - 8\hat{j} - \hat{k}}{\sqrt{185}}$ ()

3. The d.c.'s of a unit vector which is equally inclined to the coordinate axes are

(a)
$$(1, 1, 1)$$
 (b) $(\frac{1}{3}, \frac{1}{3}, \frac{1}{3})$ (c) $(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}})$ (c) $(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}})$ (c) (d) $(1, 0, 0)$ (d) $(1, 0, 0)$ (d) $(1, 0, 0)$

4. The unit vector perpendicular to the plane of the vectors $\vec{a} = 2\hat{i} - 6\hat{j} - 3\hat{k}$ and $\vec{b} = 4\hat{i} + 3\hat{j} - \hat{k}$ is

(a)
$$\pm \frac{(2\hat{i} - 6\hat{j} - 3\hat{k})}{\sqrt{7}}$$
 () (b) $\pm \frac{(2\hat{i} - 6\hat{j} + 3\hat{k})}{\sqrt{7}}$ ()

(c)
$$\pm \frac{(3\hat{i}-2\hat{j}+6\hat{k})}{7}$$
 () (d) $\pm \frac{(3\hat{i}-6\hat{j}+2\hat{k})}{7}$ ()

5. The value of λ in which the four points with position vectors $(-6\hat{i}+3\hat{j}+2\hat{k})$, $(3\hat{i}+\lambda\hat{j}+4\hat{k})$, $(5\hat{i}+7\hat{j}+3\hat{k})$ and $(-13\hat{i}+17\hat{j}-2\hat{k})$ are coplanar is (b) -1 (d) -2 (a)1 ())) (c)2)

- A vector $\vec{\mathbf{V}}$ is irrotational if 6.
 - (a) $\nabla \cdot \vec{\mathbf{V}} = \mathbf{0}$ () (b) $\nabla \times \vec{\mathbf{V}} = 0$ ()

- (c) $\nabla \cdot \vec{\mathbf{V}}$ is always positive ()
- (d) $\nabla \times \vec{\mathbf{V}}$ is always positive ()
- 7. If $\phi(x, y, z) = c$ represents a surface, then $\nabla \phi$ is a) a vector tangential to the surface ϕ () b) always a unit normal to the surface ϕ () c) a vector perpendicular to the surface ϕ () d) none of the above. ()
- 8. If $\vec{F} = \nabla \phi$, where ϕ is a single valued function and has continuous partial derivatives, then $\int_C \vec{F} \cdot d\vec{r}$
 - a) depends on the path C. ()
 - b) is independent of the path C ()
 - c) does not exist ()
 - d) none of the above ()
- 9. If \vec{F} is a conservative field, then
 - (a) $\nabla \times \vec{\mathbf{V}} = 0$ ()
 - (b) $\nabla \cdot \vec{\mathbf{V}} = 0$ ()
 - (c) $\nabla \cdot \vec{\mathbf{V}}$ is always positive ()
 - (d) $\nabla \times \vec{\mathbf{V}}$ is always positive ()

10. The directional derivatives of $\phi = 4xz^3 - 3x^2y^2z$ at (2,-1,2) in the direction of (2,-3,6) is

a) 367/7 ()
b) 357/7 ()
c) 386/7 ()
d) 376/7 ()

11. If by any change of axes, without change of origin, the quantity a $x^2 + 2hxy + by^2 + 2gx + 2fy + c$ transforms to $a'x'^2 + 2h'x'y' + b'y'^2 + 2g'x' + 2f'y' + c'$ then

(a)
$$a + b = a' + b'$$
 (b) $ab + h^2 = ab + h^2 = a'b' + h'^2$ (c)
(c) $f^2 - g^2 = f'^2 - g'^2$ (c) (d) None of these. (c)

12. By a parallel transformation the origin is shifted to the point (a, b), then the equation $\frac{x}{a} + \frac{y}{b} = 2$ transforms into

(a)
$$\frac{x}{a} + \frac{y}{b} = 1$$
 (b) $\frac{x}{a} + \frac{y}{b} = 4$ (c)

(c)
$$\frac{x}{a} + \frac{y}{b} = 2$$
 (d) $\frac{x}{a} + \frac{y}{b} = 0$ (d)

13. The equation of lines passing through the origin and perpendicular to $5x^2 - 7xy - 3y^2 = 0$ is

(a)
$$7x^2 - 3xy - 5y^2 = 0$$
 (b) $3x^2 - 7xy - 5y^2 = 0$ (c)
(c) $7x^2 + 3xy - 5y^2 = 0$ (c) (d) $3x^2 + 7xy - 5y^2 = 0$ (c)

14. The angle between the lines joining the origin to the points common to $5x^2 + 12xy - 8y^2 + 8x - 4y + 12 = 0$ and x - y = 2 is

- (a) $\tan^{-1}\frac{3}{4}$ (b) $\tan^{-1}-\frac{3}{4}$ (c)
- (c) $\tan^{-1}\frac{4}{3}$ () (d) $\tan^{-1}-\frac{4}{3}$ ()

15. The pole of the straight line x + 2y + 3 = 0 w.r.t. the conic $x^2 + y^2 - 2x + 5 = 0$ is

- (a) (1, 1) (b) (1, 2) ()
- (c) (2, 1) () () (d) (2, 2) ()

16. If a plane meets the axes in A, B, C and the centroid of triangle ABC is (α, β, γ) , then the equation of the plane is

(a)
$$\frac{x}{\alpha} + \frac{y}{\beta} + \frac{z}{\gamma} = 0$$
 (b) $\frac{x}{\alpha} + \frac{y}{\beta} + \frac{z}{\gamma} = 1$ (c)

17. The distance of the point (4, 3, 5) from xz – plane is (a) 4 units () (b) 3 units () (c) 5 units () (d) 0 unit () 18. The equation of the plane which contains the lines $\frac{x-1}{2} = -y-1 = \frac{z-3}{4}$ and is perpendicular to the plane x + 2y + z = 12 is (a) 9x - 2y - 5z + 4 = 0 () (b) 2x - 9y - 4z + 5 = 0 () (c) 9x + 2y - 5z + 4 = 0 () (d) 2x + 9y - 4z - 5 = 0 () 19. The perpendicular distance of P(1, 2, 3) from the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$ is (a) 4 () (b) 5 () (c) 6 () (d) 7 () 20. The image of the point (1, 3, 4) in the plane 2x - y + z + 3 = 0 is (a) (-3, 5, 2) () (b) (3, -5, 2) () (c) (3, 5, -2) () (d) (3, 5, 2) () 21. The centre of the sphere $x^2+y^2+x^2-8y+10z-10 = 0$ is (a) (-4, -5) (b) (3, -5, 2) () (c) (-3, 5, 2) () 22. The greatest distance from the point (1, -1, 2) to the sphere $x^2+y^2+z^2-4x+6y-8z-71 = 0$ is (c) 13 () (f) 11 () (g) 9 () h) 7 () 23. All generator of the cylinder f(x,y) = 0 are parallel to (a) X-axis () (b) Y-axis () (c) Z-axis ()	(c) $\frac{x}{\alpha} + \frac{y}{\beta} + \frac{z}{\gamma} = 2$	()		(d) $\frac{x}{\alpha} + \frac{y}{\beta} + \frac{z}{\gamma} = 3$	()
(a) 4 units () (b) 3 units () (c) 5 units () (d) 0 unit () 18. The equation of the plane which contains the lines $\frac{x-1}{2} = -y-1 = \frac{z-3}{4}$ and is perpendicular to the plane $x + 2y + z = 12$ is (a) $9x - 2y - 5z + 4 = 0$ () (b) $2x - 9y - 4z + 5 = 0$ () (c) $9x + 2y - 5z + 4 = 0$ () (d) $2x + 9y - 4z - 5 = 0$ () 19. The perpendicular distance of P(1, 2, 3) from the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$ is (a) 4 () (b) 5 () (c) 6 () (d) 7 () 20. The image of the point (1, 3, 4) in the plane $2x - y + z + 3 = 0$ is (a) (-3, 5, 2) () (b) (3, -5, 2) () (c) (3, 5, -2) () (d) (3, 5, 2) () 21. The centre of the sphere $x^2+y^2+z^2-8y+10z-10 = 0$ is (e) (0,4,5) (f) (0,4,-5) (g) (0,-4,5) (h) (0,-4,-5) 22. The greatest distance from the point (1,-1,2) to the sphere $x^2+y^2+z^2-4x+6y-8z-71 = 0$ is (e) 13 () (f) 11 () (g) 9 () (h) 7 () 23. All generator of the cylinder f(x,y) = 0 are parallel to (a) X-axis () (b) Y-axis () (c) Z-axis () (c) Z-axis () (c) Z-axis () (c) X-axis () (c)	17. The distance of the	e point (4, 3	, 5) from	$n xz - p^{2}$	ane is		
(c) 5 units () (d) 0 unit () 18. The equation of the plane which contains the lines $\frac{x-1}{2} = -y-1 = \frac{z-3}{4}$ and is perpendicular to the plane $x + 2y + z = 12$ is (a) $9x - 2y - 5z + 4 = 0$ () (b) $2x - 9y - 4z + 5 = 0$ () (c) $9x + 2y - 5z + 4 = 0$ () (d) $2x + 9y - 4z - 5 = 0$ () 19. The perpendicular distance of P(1, 2, 3) from the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$ is (a) 4 () (b) 5 () (c) 6 () (d) 7 () 20. The image of the point (1, 3, 4) in the plane $2x - y + z + 3 = 0$ is (a) (-3, 5, 2) () (b) (3, -5, 2) () (c) (3, 5, -2) () (d) (3, 5, 2) () 21. The centre of the sphere $x^2+y^2+z^2-8y+10z-10 = 0$ is (a) (-4, -5) (c) (0, 4, -5) (c) (0, 4, -5) (c) (1) (1) (1) (2) 22. The greatest distance from the point (1, -1, 2) to the sphere $x^2+y^2+z^2-4x+6y-8z-71 = 0$ is (c) (1) (1) (2) (c) (3, 5, -2) () (2) (3) (3, 5, 2) () 23. All generator of the cylinder f(x, y) = 0 are parallel to (c) (3, -xais ()) (c) (2, -axis ())	(a) 4 units	()		(b) 3 units	()
18. The equation of the plane which contains the lines $\frac{x-1}{2} = -y-1 = \frac{z-3}{4}$ and is perpendicular to the plane $x + 2y + z = 12$ is (a) $9x - 2y - 5z + 4 = 0$ () (b) $2x - 9y - 4z + 5 = 0$ () (c) $9x + 2y - 5z + 4 = 0$ () (d) $2x + 9y - 4z - 5 = 0$ () (1) 19. The perpendicular distance of P(1, 2, 3) from the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$ is (a) 4 () (b) 5 () (c) 6 () (c) 7 () (c) 6 () (c) 6 () (c) 7 () (c) 6 () (c) 7	(c) 5 units	()		(d) 0 unit	()
to the plane $x + 2y + z = 12$ is (a) $9x - 2y - 5z + 4 = 0$ () (b) $2x - 9y - 4z + 5 = 0$ () (c) $9x + 2y - 5z + 4 = 0$ () (d) $2x + 9y - 4z - 5 = 0$ () 19. The perpendicular distance of P(1, 2, 3) from the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$ is (a) 4 () (b) 5 () (c) 6 () (d) 7 () 20. The image of the point (1, 3, 4) in the plane $2x - y + z + 3 = 0$ is (a) (-3, 5, 2) () (b) (3, -5, 2) () (c) (3, 5, -2) () (d) (3, 5, 2) () 21. The centre of the sphere $x^2+y^2+z^2-8y+10z-10 = 0$ is (a) (0, 4, 5) (b) (0, -4, -5) (c) (1, -4, -5) (c) (2, 3, 1, -2) () (2, -4, -5) (c) (3, 2, -2) () (3, -5, 2) () (c) (3, 2, -2) () (3, -5, 2) () (c) (3, 5, -2) () (3, -5, 2) () (c) (3, -5, 2) () (3, -5, 2) () (c) (3, -5, 2) () (3, -5, 2) () (c) (3, -5, 2) () (3, -5, 2) () (c) (3, -5, 2) () (3, -5, 2) () (c) (3, -4, 5) () (3, -5, 2) () (c) (3, -4, 5) () (3, -5, 2) () (c) (3, -4, 5) () (3, -5, 2) () (3, -5, 2) () (c) (3, -4, 5) () (3, -5, 2)	18. The equation of th	e plane whic	h contair	ns the li	nes $\frac{x-1}{2} = -y - 1 = \frac{z-3}{4}$ and	is perpe	ndicular
(a) $9x - 2y - 5z + 4 = 0$ () (b) $2x - 9y - 4z + 5 = 0$ () (c) $9x + 2y - 5z + 4 = 0$ () (d) $2x + 9y - 4z - 5 = 0$ () 19. The perpendicular distance of P(1, 2, 3) from the line $\frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$ is (a) 4 () (b) 5 () (c) 6 () (d) 7 () 20. The image of the point (1, 3, 4) in the plane $2x - y + z + 3 = 0$ is (a) (-3, 5, 2) () (b) (3, -5, 2) () (c) (3, 5, -2) () (d) (3, 5, 2) () 21. The centre of the sphere $x^2 + y^2 + z^2 - 8y + 10z - 10 = 0$ is (c) (0, 4, 5) (c) (0, 4, -5) (c) (1, 4, -5) (c) (2, 5, -2) () (2, -2) () 22. The greatest distance from the point (1, -1, 2) to the sphere $x^2 + y^2 + z^2 - 4x + 6y - 8z - 71 = 0$ is (c) (1, 2, -5) (c) (1, 2, -5) (c) (2, 3, 5, -2) () (3, 5, -2) () (c) (3, 5, -2) () (3, 5, -2) () (c) (3, 5, -2) () (3, 5, -2) () (c) (3, 5, -2) () (3, 5, -2) () (c) (3, 5, -2) () (3, -2) () (c) (3, 5, -2) () (3, -2) () (c) (3, 5, -2) () (c) (3, -2) () (c) (3, 5, -2) () (c) (3, -2) () (c) (3, 5, -2) () (c) (3, -2) () (c) (3, 5, -2) () (c) (3, -2) () (c) (3, -2, -2) () (c) (3, -2, -2) () (c) (3, -2, -2) () (c) (3, -2, -2) () (c) (-2, -2) (c) (-2, -2) (c) (c) (-2, -2) (c) (-2, -2) (c) (c) (-2, -2) (c) (-2, -2) (c) (-2, -2) (c) (c) (-2, -2) (c) (c) (-2, -2) (c) (c) (-2, -2) (c) (-2, -2) (c) (c) (-2, -2) (c) (-2,	to the plane $x + 2y + z$	z = 12 is					
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 21. The centre of the sphere x²+y²+z²-8y+10z-10 = 0 is (0,4,5) (0,4,-5) (0,-4,5) 22. The greatest distance from the point (1,-1,2) to the sphere x²+y²+z²-4x+6y-8z-71 = 0 is () () () () () () () 23. All generator of the cylinder f(x,y) = 0 are parallel to a) X-axis () b) Y-axis () 	(c) (3, 5, -2)	()		(d) (3, 5, 2)	()
	 21. The centre of t e) (0,4,5) f) (0,4,-5) g) (0,-4,5) h) (0,-4,-5) 22. The greatest di e) 13 f) 11 g) 9 h) 7 23. All generator of a) X-axis b) Y-axis c) Z-axis d) r, 1, r, 5 	<pre>he sphere x² istance from () () () (</pre>	$+y^2+z^2-8$ the point er f(x,y) =	y+10z-1	10 = 0 is) to the sphere $x^2+y^2+z^2-4x+6$ parallel to	y-8z-71	= 0 is

- 24. The angle between lines of intersection of the plane and the cone given by x-3y+z+0 and $x^2-5y^2+z^2=0$ is
- e) $\cos^{-1}(6/5)$) f) $\cos^{-1}(5/6)$ ((g) $Sin^{-1}(6/5)$) h) $Sin^{-1}(5/6)$ (25. $2x^2+2y^2+7z^2-10yz-10zx+2x+2y+26z-17 = 0$ represents a cone with vertex at a) (2,2,1) () b) (2,1,2) () c) (1,2,1) () d) (1,1,2)

Part B : Fill up the blanks

- 1. If \vec{a} is any vector then $\hat{i} \times (\vec{a} \times \hat{i}) + \hat{j} \times (\vec{a} \times \hat{j}) + \hat{k} \times (\vec{a} \times \hat{k})$ is ______.
- 2. A vector function $\vec{f}(t)$ is constant if and only if _____.
- 3. A particle moves along the curve $x = 2t^2$, $y = t^2 4t$, z = 3t 5 where t is the time. Then, the acceleration at time t = 1 is ______.

4. A vector having unit magnitude is called a ______.

5. The directional derivatives is _____ in the direction of $\nabla \phi$.

6. If \vec{F} represents the force acting on a particle moving along the path C, then the line integral over C represents the_____ by the force \vec{F} .

7. The origin is shifted to the point (3, -1) and the axes are rotated through an angle $\tan^{-1}\frac{3}{4}$. If the co-ordinates of a point are (5, 10) in the new system, its co-ordinates in the old system is

8. If axes are rotated through an angle 45° , the equation $3x^2 + 2xy + 3y^2 - 1 = 0$ is transformed into _____.

9. If pairs of lines $x^2 - 2pxy - y^2 = 0$ and $x^2 - 2qxy - y^2 = 0$ be such that each pair bisect the angles between the other pairs, then pq =_____.

10. Distance between two points $A(x_1, y_1, z_1)$ and $B(x_2, y_2, z_2)$ is given by AB =

11. Let θ be the angle between the planes $a_1x+b_1y+c_1z+d=0$ and $a_2x+b_2y+c_2z+d_2=0$. The condition of perpendicularity is _____.

12. Let a, b, c be the direction ratios of the normal to the plane through the point A (x_1, y_1, z_1) and let P(x, y, z) be any variable point on the plane. The direction ratios of AP are

- 13. Equation of sphere when centre is (α,β,γ) and the radius is r, is given by
- 14. If d is the distance between the centre of two sphere of radii r_1 and r_2 , then the angle between them is
- 15. The equation of the right circular cylinder of radius 2 whose axis is the straight line x/1 = y/-2 = z/2 is.....

Answer Key

Part A

2. (c) 2. (c) 3. (c) 4. (c) 5. (d). 6. (b) 7. (c) 8. (b) 9. (a) 10. (d) 11. (a) 12. (d) 13. (b) 14. (c) 15. (d) 16. (d) 17. (b) 18. (a) 19. (d) 20. (a) 21. (b) 22. (a) 23. (c) 24. (b) 25. (a)

Part B

2. $2\vec{a}$ 2. $\frac{df(t)}{dt} = \vec{0}$ 3. $4\hat{i} + 4\hat{j}$ 4. unit vector 5. Maximum 6. work done 7. (1,10) 8. $4x^2 + 2y^2 = 1$ 9. -1 $10.\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$ 11. $a_1a_2 + b_1b_2 + c_1c_2 = 0$ 12. $x - x_1$, $y - y_1$, $z - z_1$ 13. $(x - \alpha)^2 + (y - \beta)^2 + (z - \gamma)^2 = r^2$ 14. $\cos^{-1}\{(r_1^2 + r_2^2 - d^2)/2r_1r_2\}$ 15. $8x^2 + 5y^2 + 5z^2 + 4xy + 8yz - 4zx = 36$

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Subject: MATHEMATICS Paper name: MODERN ALGEBRA Paper No: MATH/6/CC/IX Semester: VI

A. Multiple choice questions [25 (5 from each unit)]

- 1. Which group is non-abelian of order
 - (a) 144
 - (b) 121
 - (c) 170
 - (d) 100
- 2. of the abovelf the order of a group G is p^n , where p is a prime number with centre Z, then
 - (a) Z={e}
 - (b) Z≠{e}
 - (c) Z={0}
 - (d) None
- 3. If G is a non-Abelian group pf order p^3 , where p is prime, then the order of the center Z of G is
 - (a) 1
 - (b) p
 - (c) p²
 - (d) p³
- 4. A subgroup H of a group G is normal, if it is of index
 - (a) 0
 - (b) 1
 - (c) 2
 - (d) 3
- 5. An element a of group G is self conjugate if and only if there exists x belongs to G, when
 - (a) $a^2 = ax$
 - (b) a = x
 - (c) xa = ax

(d) a = xa

- 6. The characteristic of an integral domain is either
 - (a) 0 or 1
 - (b) 0 or prime number
 - (c) 1 or composite number
 - (d) None of the above
- 7. A skew field
 - (a) Has no divisor of zero
 - (b) Is necessarily commutative
 - (c) May not possess unity element
 - (d) Has no invertible element
- 8. Which of the following is not an integral domain ?
 - (a) The ring of integers
 - (b) The ring of all 2 x 2 matrices with elements as integers
 - (c) ({ 0, 1, 2, 3, 4}, $+_5$, x_5)
 - (d) The ring of all real numbers
- 9. The ring of Gaussian integers is not
 - (a) commutative with respect to addition
 - (b) commutative with respect to multiplication
 - (c) a field
 - (d) an integral domain

10. The characteristic of the ring (I_6 , $+_6$, x_6) where $I_6 = \{0, 1, 2, 3, 4, 5\}$ is

- (a) 0
- (b) 3
- (c) 6
- (d) Infinite
- 11. The units of an integral domain Z[*i*] are
 - (a) 1,-1
 - (b) *i, -i*
 - (c) 1, -1, 0, *i*
 - (d) 1, -1, *i*, -*i*

12. Let a and b be two elements of a Euclidean ring R, then b is not a unit in R if

- (a) d(ab) < d(a)
- (b) d(ab) \geq d(a)
- (c) d(ab) = d(a)
- (d) d(ab)>(a)

13. In the ring of integers, the greatest common divisor(s) of 3 and 6 is/are

- (a) 3 and 3
- (b) 3
- (c) -3
- (d) 1

14. In the quadratic ring of integers $Z[i\sqrt{5}] = \{a + i\sqrt{5}b; a, b \in Z\}$, the number 3 is

- (a) irreducible but not prime
- (b) prime but not irreducible
- (c) irreducible and prime
- (d) neither irreducible nor prime

15. A non-zero integer has

- (a) no associate
- (b) exactly one associate
- (c) exactly two associates
- (d) infinite number of associates
- 16. Which set is a basis for the vector space $V_3(R)$?
 - (a) (1,0,0), (1,1,0), (1,1,1)
 (b) (1,0,1), (1,0,0), (0,0,1)
 (c) (1,0,0), (1,1,1)
 (d) (1,0), (0,1)

17. Which of the following set of vectors is linearly independent in $V_3(R)$?

(a) { (1,2,1), (3,1,5), (3,-4,7) }
(b) { (2,-3,1), (3,-1,5), (1,-4,3) }
(c) { (2,1,2), (8,4,8) }
(d) { (-1,2,1), (3,0,-1), (-5,4,3) }

18. If V(F) is a vector space with zero element 0 and if U and W are disjoint subspaces of V(F), then

- (a) $U \cap V = \phi$
- (b) $U \cap V = 0$
- (c) $U \cap V = \{0\}$
- (d) $U \cap V \neq 0$

19. The necessary and sufficient condition of a vector space V(F) to be a direct sum of its two subspaces U and W is

- (a) V = U + W and $U \cap W = 0$
- (b) V = UW and $U \cap W = \{0\}$
- (c) V = U + W and $U \cap W \neq \{0\}$
- (d) V = U + W and $U \cap W = \{0\}$

20. Which of the following is not a subspace of R^3 , where R is the set of all real numbers?

- (a) $S = \{(x, y, z): x + z = 0\}$
- (b) $S = \{(x, y, z): x y + 2z = 0\}$
- (c) $S = \{(x, y, z): x \le 0\}$

(d) $S = \{(x, y, z): x - 3y \in R\}$

- 21. The eigenvalues of a real symmetric matrix are
 - (a) Pure imaginary
 - (b) All real
 - (c) All zero
 - (d) None of the above
- 22. Which of the following functions T from R² into R² is a linear transformation?
 - (a) T (x₁, x₂)= (1+x₁, x₂)
 - (b) T (x_1, x_2) = (x_1^2, x_2)
 - (c) T $(x_1, x_2) = (x_1-x_2, 0)$
 - (d)) T (x_1 , x_2) = (sin x_1 , x_2)
- 23. Let $T: \mathbb{R}^3 \to \mathbb{R}^3$ be a linear transformation whose nullity is 2. Then the rank of T is
 - (a) 0
 - (b) 1
 - (c) 2
 - (d) 3

24. An n x n matrix A over the field F is diagonalizable if and only if

- (a) A has n linearly dependent eigenvectors
- (b) A has n linearly independent eigenvectors
- (c) A has n² linearly dependent eigenvectors
- (d) A has n² linearly independent eigenvectors
- 25. If T is a linear transformation from vector space $V_1(F)$ into the vector space $V_2(F)$ and
- $V_1(F)$ is finite dimensional of dimension n then
 - (a) rank (T) + nullity (T) = n
 - (b) rank (T) + nullity (T) = 1
 - (c) rank (T) + nullity (T) = n^2
 - (d) rank (T) + nullity (T) = n^n .

Fill up the blanks [15 (3 from each unit)]

- 1. A group having no proper subgroup is called ______
- 2. Every subgroup of an abelian group is _____
- 3. Every homomorphic image of a group G is ______ to some quotient

group of G.

- The characteristic of an integral domain is either ______ or a prime number.
- 5. A commutative ring with unity is a ______ if it has no proper ideal.
- An ideal S of a commutative ring R is ______ if and only if the residue class ring R/S is a field.
- 7. In any commutative ring with unity, the associate of 0 is only ______.

8. An ideal S of the Euclidean ring R is maximal iff S is generated by some

_____ of R.

- 9. Every Euclidean ring possesses ______ elements.
- 10. If two vectors are linearly dependent, one of them is a ______ of the

other.

- 11. There exists a ______ for each finite dimensional vector space.
- 12. Two finite dimensional vector spaces are isomorphic iff they are of the ______.
- 13. Any system consisting of a single non-zero vector is always linearly ______.
- 14. Similar matrices have the same ______.
- 15. An n x n matrix A over the field F is diagonalizable iff A has ______

eigenvectors.

Key Answ	ers					
A. Multipl	e choice questi	ions				
1. (c)	2. (b)	3. (b)	4. (c)	5. (c)	6. (b)	7. (a)
8. (b)	9. (c)	10. (c)	11. (d)	12.(d)	13. (a)	14. (a)
15. (c)	16.(a)	17. (b)	18. (c)	19. (d)	20. (c)	21.(b)
22. (c)	23. (b)	24.(b)	25. (a)			

B. Fill up the blanks

- 1. Simple group
- 2. Normal
- 3. Isomorphic
- 4. Zero
- 5. Field
- 6. Maximal
- 7. Zero
- 8. Prime element
- 9. Unity
- 10. Scalar multiple
- 11. Basis
- 12. Same dimension
- 13. Independent
- 14. Eigenvalues
- 15. n linearly independent

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Subject : MATHEMATICS Paper name : Advanced Calculus Paper No : MATH/6/CC/X Semester : VI

A. Multiple choice questions

1. If f is integrable on [a, b], then |f| is integrable and

a)
$$\left| \int_{a}^{b} f \, dx \right| \leq \int_{a}^{b} |f| \, dx$$

b)
$$\left| \int_{a}^{b} f \, dx \right| \ge \int_{a}^{b} |f| \, dx$$

c) $\left| \int_{a}^{b} f \, dx \right| = \int_{a}^{b} |f| \, dx$ are always equal

c)
$$\left| \int_{a}^{b} f \, dx \right|$$
 and $\int_{a}^{b} |f| \, dx$ are always equal
d) None of the above

2. For a bounded and integrable function f, if $b \ge a$, then

a)
$$m(b-a) < \int_{a}^{b} f \, dx < M(b-a)$$

b)
$$m(b-a) \ge \int_a^b f \, dx \ge M(b-a)$$

c)
$$m(b-a) \le \int_a^b f \, dx \le M(b-a)$$

d)
$$m(b-a) > \int_{a}^{b} f \, dx > M(b-a)$$

3. If P and S are any two partitions of [a,b], then

a) $L(P, f) \le U(S, f)$

b)
$$U(S,f) \le L(P,f)$$

c)
$$U(S,f) \le U(P,f)$$

d)
$$U(P,f) \le U(P,f)$$

4. If P* is a refinement of P, then for a bounded function f,

- a) $L(P^*, f) \leq L(P, f)$
- b) $L(P^*, f) \ge L(P, f)$
- c) $U(P^*, f) \ge U(P, f)$

d) None of the above

5. The lower Riemann integral for a function f corresponding to the partition P of the interval [a,b] is given by

a)
$$\sup U(P, f) = \int_{\bar{a}}^{b} f(x) dx$$

b) $\inf L(P, f) = \int_{\bar{a}}^{b} f(x) dx$
c) $\inf U(P, f) = \int_{\bar{a}}^{b} f(x) dx$
d) $\sup L(P, f) = \int_{\bar{a}}^{b} f(x) dx$

6. The improper integral $\int_a^b \frac{1}{(x-a)^n} dx$ is convergent if and only if

- a) *n* > 1 b) *n* < 1
- c) n = 1

7. If f and g are two positive functions on [a,b] such that

$$\lim_{x \to a^+} \frac{f(x)}{g(x)} = l$$

Where *l* is a non-zero finite number, then

a)	$\int_{a}^{b} f dx$ converges if $\int_{a}^{b} g dx$ converges	
b)	$\int_{a}^{b} g dx$ converges if $\int_{a}^{b} f dx$ diverges	
c)	$\int_{a}^{b} f dx$ converges if $\int_{a}^{b} g dx$ diverges	
d)	$\int_{a}^{b} g dx$ converges does not need to imply $\int_{a}^{b} f dx$ converges.	

8. The improper integral $\int_a^{\infty} \frac{1}{x^n} dx$ is convergent if and only if

- a) *n* > 1 b) *n* < 1 c) *n* = 1
- d) None of the above

9. If f and g are two positive functions on [a,b] such that $f(x) \leq g(x) \forall x \in [a,b]$, then

a)	$\int_{a}^{b} f dx$ converges if $\int_{a}^{b} g dx$ converges	
b)	$\int_{a}^{b} g dx$ converges if $\int_{a}^{b} f dx$ diverges	
c)	$\int_{a}^{b} f dx$ converges if $\int_{a}^{b} g dx$ diverges	

d) $\int_{a}^{b} g \, dx$ converges does not need to imply $\int_{a}^{b} f \, dx$ converges. 10. The integral $\int_0^\infty x^{n-1} e^{-x} dx$ converges if and only if a) *n* < 0 b) n = 0c) n > 0d) $n \leq 0$ 11. Suppose f is continuous function of two variables with domain as rectangle $[a, b; c, d] \subset \mathbb{R}^2$. Then the function $\phi(y) = \int_a^b f(x, y) dx$ for a fixed value of $y \in [c, d]$ is a) discontinuous in [c, d]b) derivable even though f_y does not exists and continuous c) continuous in [c, d]d) none of the above 12. The value of the integral $\int_0^\infty \frac{tan^{-1}ax}{x(1+x)^2} dx$ if a > 0 is a) $\frac{\pi}{2}$ b) $-\frac{\pi}{2}$ c) $\frac{\pi}{2(1+a)}$ d) $\frac{\pi}{2}\log(1+a)$ 13. The value of the improper integral $\int_0^\infty e^{-x^2} dx$ is a) $\frac{\pi}{2}$ b) $\sqrt{\frac{\pi}{2}}$ c) $\frac{\pi}{\sqrt{2}}$

d)
$$\frac{\sqrt{\pi}}{2}$$

14. The uniformly convergent improper integral of a continuous function

a) is not continuous	
b) is itself continuous	
c) may be continuous	
d) none of the above	

15. If *f* is a continuous function when $c \le y \le d$, $x \ge a$; and the integral $\phi(y) = \int_a^{\infty} f(x, y) dx$ is uniformly convergent, then

a)
$$\int_{c}^{d} \left\{ \int_{a}^{\infty} f(x, y) dx \right\} dy = \int_{c}^{d} \phi(y) dy = \int_{a}^{\infty} \left\{ \int_{c}^{d} f(x, y) dy \right\} dx$$

$$b)\int_{c}^{a} \left\{ \int_{a}^{\infty} f(x, y) dx \right\} dy \neq \int_{c}^{a} \phi(y) dy \qquad \Box$$

c)
$$\int_{a}^{\infty} \left\{ \int_{c}^{a} f(x, y) dy \right\} dx \neq \int_{c}^{a} \phi(y) dy$$

d)
$$\int_{c}^{d} \left\{ \int_{a}^{\infty} f(x, y) dx \right\} dy \neq \int_{a}^{\infty} \left\{ \int_{c}^{d} f(x, y) dy \right\} dx$$

16. The integral $\int_c xy \, dx$ along the arc of a parabola $x = y^2$ from (1,-1) to (1,1) is

- a) 3 □ b) 4/5 □
- c) 2/3
- d) 2
- 17. The integral $\int_c (x^2 y dx + x y^2 dy)$ where C is the line segment from (1,0) to (0,1) is
 - a) -2/3 b) 1/6 c) 2/3 d) 0

18. The value of the double integral

a) 0

$$-\frac{1}{2}$$
c) $\frac{1}{2}$
d) 1
$$\int_{00}^{11} \frac{x-y}{(x+y)^3} dx dy \text{ is}$$

$$\square \text{ b)}$$

$$\square$$

19. The value of $\int_C (2x^2 + y^2)dx + 3(y - 4x)dy$ where the path C is a triangle PQR with P(0,0), Q(2,0) and R(0,2)

a) 23/60	□ b)
-23/60	
c) -80/3	
d) 80/3	

20. Choose the correct one

a) $\int_{-C} f dx + g dy = -\int_{C} f dx + g dy$			b)
$\int_{-C} f dx + g dy = -\int_{-C} f dx + g dy$			
c) $\int_{-C} f dx + g dy = - \int_{-C} f dx - g dy$			
a) $\int_{-c} f dx + g dy = \int_{c} f dx + g dy$			
21. The sequence of function $\{f_n\}$ where $f_n(x) = x^n$ is			
 a) Neither pointwise nor uniformly continuous for x ∈ [0,1] b) Pointwise continuous for x ∈ [0,1] c) Uniformly continuous for x ∈ [0,1] d) None of the above 			
22. The series $\sum_{n=1}^{\infty} \frac{1}{n^p}$ is uniformly continuous if			
a) $p < 1$ b) $p = 1$ c) $p > 1$ d) $p \le 1$			
23. The sequence of function $\{f_n\}$ where $f_n(x) = \frac{n}{x+n}$ is			
a) uniformly convergent in $[0, \infty)$			
b) uniformly convergent in $[0, k]$ where k is any finite number.			
c) nowhere convergent.			
d) none of the above.			
24. The sequence of function $\{f_n\}$ where $f_n(x) = \frac{n}{1+nx} \forall x \in [0,1]$			
a) diverges			
b) converges but not uniformly.			
c) converges pointwise only			
d) converges uniformly			
25. If a sequence of function $\{f_n\}$ are continuous and uniformly convergent and on [a,b], then	converg	ges to j	f

b) f is differentiable on $[a, b]$	
c) <i>f</i> is continuous on [<i>a</i> , <i>b</i>]	
d) none of the above	

B. Fill in the blanks

1. If P* is a refinement of P, then for a bounded function f, then $U(P^*, f) __U(P, f)$.

2. By Darboux's theorem, if f is a bounded function on [a,b], then for every $\epsilon > 0$, there exist $\delta > 0$, such that for every partition P on [a,b], with norm $\mu(P) < \delta$,_____.

3. Every continuous function is _____

4. Every ______ convergent integral in [*a*, *b*] is convergent in [*a*, *b*].

5. If f and g are two positive functions on [a, b] such that

$$\lim_{x \to a^+} \frac{f(x)}{g(x)} = l$$

where *l* is non-zero finite number, then the two integrals $\int_a^b f dx$ and $\int_a^b g dx$ ______ together at *a*.

6. The improper integral $\int_{a}^{\infty} f(x) dx$ is said to be absolutely convergent if ______ is convergent.

7. Let f(x, y) be a continuous function an let $\phi(y) = \int_a^b f(x, y) dx$, if f_y exists and is continuous in [a, b; c, d], then ϕ is _____ and

$$\phi'(y) = \int_{a}^{b} f_{y}(x, y) dx \quad \forall y \in [c, d]$$

8. If |a| < 1, then show that

$$\int_{0}^{n} \frac{\log(1 + a\cos x)}{\cos x} dx = \underline{\qquad}$$

9. ______improper integral of a continuous function is a continuous function.

10. If f(x,y) is ______ over a rectangle R defined by $a \le x \le b$; $c \le y \le d$, then

$$\iint_{ac}^{bd} f(x,y)dydx = \iint_{ca}^{db} f(x,y)dxdy$$

11. Ellipse is a _____curve.

12. The value of the double integral

$$\iint_{00}^{11} \frac{x - y}{x + y} dx dy \text{ is } ____$$

- 13. The necessary and sufficient condition for uniform convergence of a sequence of function $\{f_n(x)\}$ on a domain [a, b] is that for every $\epsilon > 0$ there exist a +ve integer 'n' such that _____, $\forall n \ge m, x \in [a, b]$ and $\forall p \in \mathbb{N}$
- 14. The sum of a uniformly convergent series of a continuous function is ______.
- 15. The function $f_n(x) = nx e^{-nx^2}$ is _____ convergent on $[0, \infty)$.

Answer Key

A. Multiple choice questions

 1. a)
 2. c)
 3. a)
 4. b)
 5. d)
 6. b)
 7. a)
 8. a)
 9. a)
 10. c)
 11. c)
 12. d)
 13.

 d)
 14. b)
 15. a)
 16. b)
 17. d)
 18. b)
 19. c)
 20. a)
 21. b)
 22. c)
 23. c)
 24. d)
 25.

 b)

B. Fill in the blanks

1.≥

2.
$$U(P,f) < \int_a^{\overline{b}} f(x) dx + \epsilon$$

- 3. integrable
- 4. absolute
- 5. converge and diverge

6.
$$\left|\int_{a}^{\infty} f(x)dx\right|$$

7. derivable

8. $\pi sin^{-1}a$

- 9. Uniformly convergent
- 10. continuous
- 11. Jordan/simple closed
- 12. 0 (zero)
- 13. $\left|f_{n+p}(x) f_n(x)\right| < \epsilon$
- 14. continuous
- 15. pointwise

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Subject : Mathematics Paper Name: Mechanics Paper No. : MATH/6/CC/XI Semester : VI

SECTION – A Multiple Choice

UNIT – I

- 1. Three coplanar forces acting on a rigid body is in equilibrium if
 - (a) two of them form a couple
 - (b) the resultant R vanishes
 - (c) all three meet at a point
 - (d) two of them meet at a point
- 2. If α and λ be the angle of inclination of an inclined plane and the angle of friction, then a body of weight W cannot rest on the inclined plane if
 - (a) $a > \lambda$
 - (b) $a = \lambda$
 - (c) $a < \lambda$
 - (d) $a \neq \lambda$
- 3. The equation of the resultant of any number of coplanar forces acting on a rigid body is given by
 - (a) $xR_x yR_y = G$
 - (b) $G + xR_x yR_y = 0$
 - (c) $G + xR_y yR_x = 0$
 - (d) $xR_y yR_x = G$
- 4. If a body of weight W is placed on a rough inclined plane inclined at an angle α to the horizon be acted on by a force P at an angle θ to the plane. Then the body is just on the point of slipping down if

(a) $P = W \frac{\sin(\alpha - \lambda)}{\cos(\theta + \lambda)}$ (b) $P = W \frac{\sin(\alpha + \lambda)}{\cos(\theta - \lambda)}$ (c) $P = W \frac{\sin(\theta + \lambda)}{\cos(\alpha - \lambda)}$ (d) $P = W \frac{\sin(\theta - \lambda)}{\cos(\alpha + \lambda)}$

5. If a body rests in limiting equilibrium on a rough inclined plane for which the coefficient of friction is $\frac{1}{4}$, then the angle of friction is

(a)
$$\frac{\pi}{2} + \tan^{-1}\left(\frac{1}{4}\right)$$

(b) $\pi + \tan^{-1}\left(\frac{1}{4}\right)$
(c) $\tan^{-1}\left(\frac{1}{4}\right)$

(d) None of the above

UNIT - II

6. The centre of gravity of a semi-circular arc is given by

(a)
$$\left(\frac{a}{\pi}, 0\right)$$

(b) $\left(\frac{2a}{\pi}, 0\right)$
(c) $\left(\frac{3a}{\pi}, 0\right)$
(d) $\left(\frac{4a}{\pi}, 0\right)$

7. The centre of gravity of a circular arc of radius 4 cm subtending at an angle 90° lies on the axis of symetry at a distance of

(a)
$$\frac{2\sqrt{2}}{\pi}$$
 from the centre
(b) $\frac{4\sqrt{2}}{\pi}$ from the centre
(c) $\frac{6\sqrt{2}}{\pi}$ from the centre
(d) $\frac{8\sqrt{2}}{\pi}$ from the centre

- 8. The centre of gravity of three uniform rods forming a triangle is at
 - (a) the centroid of the triangle
 - (b) the orthocentre of the triangle
 - (c) the incentre of the triangle
 - (d) none of the above
- 9. If the length of the median AD of a triangle ABC is 6 cm. Then the distance of the C.G. from the vertex A is
 - (a) 2 cm
 - (b) 3 cm
 - (c) 4 cm

(d) 5 cm

- 10. The centre of gravity of a triangular lamina is at
 - (a) the centroid of the triangle
 - (b) the orthocentre of the triangle
 - (c) the incentre of the triangle
 - (d) none of the above

UNIT - III

- 11. If the angular velocity of a point moving in a plane curve be constant about a fixed origin, then
 - (a)transverse acceleration is perpendicular to its velocity
 - (b) transverse acceleration varies as its radial velocity
 - (c) radial acceleration varies as its radial velocity
 - (d) radial acceleration is perpendicular to its velocity
- 12. If time t be regarded as a function of velocity v, then the rate of decrease of acceleration is given by

(a)
$$f^4 \frac{d^2 t}{dv^2}$$

(b)
$$f^3 \frac{d^2 t}{dv^2}$$

(c) $f^2 \frac{d^2 t}{dv^2}$

(d)
$$f \frac{d t}{dv^2}$$

13. If the maximum velocity of a body moving with SHM is 6cm/sec and its period is $\frac{1}{3}$ sec,

then its amplitude is given by

(a)
$$\frac{1}{\pi}cm$$

(b) $\frac{2}{\pi}cm$
(c) $\frac{1}{2\pi}cm$
(d) $\frac{1}{4\pi}cm$

14. If a particle moves in a plane with constant speed, then

- (a) its acceleration is perpendicular to its velocity
- (b) its acceleration is parallel to its velocity
- (c) its acceleration is zero
- (d) none of the above

15. For a particle executing SHM of period $\frac{\pi}{10}$ sec and amplitude 5 cm, the maximum velocity

attained is

- (a) 5 cm/sec
- (b) 50 cm/sec
- (c) 10 cm/sec
- (d) 100 cm/sec

UNIT-IV

- 16. If a particle is projected with a velocity 7m/s from the ground at an angle α with the horizontal, then the velocity of the particle at height $\frac{1}{19.6}$ is
 - (a) $4\sqrt{3} m/s$
 - (b) $5\sqrt{3} m/s$
 - (c) $6\sqrt{3} m/s$
 - (d) $7\sqrt{3} m/s$
- 17. The maximum range down an inclined plane is

(a)
$$\frac{u^2}{g(1-\cos\beta)}$$

(b)
$$\frac{u^2}{g(1+\cos\beta)}$$

(c)
$$\frac{u^2}{g(1-\sin\beta)}$$

(d)
$$\frac{u^2}{g(1+\sin\beta)}$$

18. For a given velocity of projection, the range down an inclined plane is 5 times the range up the inclined plane, then the inclination of the plane to the horizontal is

(a)
$$\sin^{-1}\left(\frac{1}{2}\right)$$

(b) $\sin^{-1}\left(\frac{2}{3}\right)$

(c)
$$\sin^{-1}\left(\frac{1}{3}\right)$$

(d) $\sin^{-1}\left(\frac{3}{2}\right)$

- 19. If the equation of motion of a body falling under gravity in a resisting medium is, then the terminal velocity is
 - (a) the initial velocity
 - (b) the least velocity attained
 - (c) the velocity when the acceleration is greatest
 - (d) the maximum velocity attained
- 20. If u and be the velocity and angle of projection, then the time taken to reach its greatest height is given by

(a)
$$t = \frac{u \sin \alpha}{g}$$

(b) $t = \frac{u \cos \alpha}{g}$
(c) $t = \frac{u \tan \alpha}{g}$
(d) $t = \frac{u \cot \alpha}{g}$

UNIT - V

- 21. A sphere of mass m strikes a plane normally with velocity u and is rebounded. If e is the coefficient of restitution, then the loss of K.E. due to the impact is
 - (a) $\frac{1}{2}me^{2}u^{2}$ (b) $\frac{1}{2}mu^{2}$ (c) $\frac{1}{2}m(1+e^{2})u^{2}$ (d) $\frac{1}{2}m(1-e^{2})u^{2}$
- 22. A sphere of mass *m* impinges on a fixed plane with velocity *u* at an angle with the normal and is rebounded. If *e* is the coefficient of restitution, then the impulse of the blow is (a) $mu(1+e)\cos\alpha$
 - (b) $mu(1+e)\sin\alpha$

- (c) $mu(1-e)\cos\alpha$
- (d) $mu(1-e)\sin\alpha$
- 23. If the earth's attraction on a particle varies inversely as the square of its distance from the earth's centre and if the radius of the earth is *a* Km, then the work done by the earth's attraction on a particle of weight 6 Kg on the surface of the earth is
 - (a) *3a*
 - (b) *4a*
 - (c) 5*a*
 - (d) 6a

24. For a perfectly elastic impact, the coefficient of restitution 'e' equals

- (a) -1
- (b) 1
- (c) 2
- (d) 0

25. A smooth sphere impinges directly with a velocity u on another smooth sphere of equal mass at rest. If the spheres are perfectly elastic, then the velocity of the second sphere is

- (a) 0
- (b) $\frac{1}{2}u$
- (c) *u*
- (d) 2*u*

SECTION – B Fill in the blanks

UNIT – I

- 1. In case of limiting equilibrium of a body on a rough surface, if F be the limiting friction at the point of contact, R the normal reaction between the bodies and μ the coefficient of friction, then $\mu = _$ _____
- 2. If three forces of magnitude 1P, 5P and 7P act along the side of an equilateral triangle ABC, then the magnitude of the resultant is _____
- 3. If three forces acting on a rigid body be in equilibrium, then they must be _____

UNIT – II

4. The centre of gravity of a hemispherical surface of radius *a* is on the axis at a distance ______ from the centre.

- 5. The moment of inertia of a circular disc of radius r about an axis through its centre perpendicular to its plane is _____
- 6. The centre of gravity of a semi-circular lamina of radius *a* is at a distance ______ from the centre.

UNIT – III

- 7. An oscillatory periodic motion is known as _____
- 8. The maximum displacement of a particle from the mean position is called the ______ of the motion.
- 9. The number of complete oscillations in one second is called the ______

UNIT – IV

- 10. The path of a projectile is known as the _____
- 11. If *u* be the velocity of projection, then the maximum horizontal range is _____
- 12. The distance between the point of projection and the point where the particle strikes the horizontal plane through the point of projection is called the _____

UNIT - V

- 13. Two equal and perfectly elastic spheres interchange their ______ after impact.
- 14. The phenomenon of two or more bodies colliding with or striking against or impinging on each other is called ______
- 15. If a particle moves so that its normal acceleration is always zero, then the path is a _____

Answer key Section A	<i>y</i>					
1. (b)	2. (a)	3.(d)	4.(a)	5. (c)	6.(b)	7.(d)
8.(c)	9.(c)	10.(a)	11.(b)	12.(d)	13.(a)	14.(c)
15.(b)	16.(a)	17.(c)	18.(b)	19.(d)	20.(a)	21.(d)
22.(a)	23. (c)	24.(b)	25.(c)			
Section – B						
1. $\frac{F}{-}$	2. $2\sqrt{7}P$	3. coplanar	4. $\frac{a}{a}$	5. $\frac{1}{2}Mr^2$	6. $\frac{4a}{2}$	

R $2 + 2\sqrt{11}$ $3 + 2\sqrt{11}$ 3π 7. Simple Harmonic Motion (SHM)8. amplitude9. frequency10. trajectory11. $\frac{u^2}{g}$ 12. range13. velocities14. impact

15. hyperbola

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Subje Pape Pape	ect : M r Nam r No. :	athematics e: Computer MATH/6/CC	Programi /XIIC	ming in	с					
Jenne	ester .	Part A	:Tick (√) †	the corr	rect ans	wer in th	ne brack	kets provide	ed:	
1	. The	number of ke	eywords a	vailable	e in C is					
	(a)	30	()		(b)	31		()
	(c)	32	()		(d)	33		()
2	. Sup	pose a = 14 a	nd b = 4 ,	what w	vill be th	ne result	ofa%t	o ?		
	(a)	1	()		(b)	2		()
	(c)	3	()		(d)	4		()
3	. Evei	ry C programi	ming mus	t contai	ins only	one :				
	(a)	printf () fu	inction		()	(b)	exit ()f	unction	
	(c)	scanf () fu)	nction		()	(d)	main ()	function	(
4	. Whi	ch one of the	following	g is the	proper	declarati	ion of a	pointer ?		
	(a)	* x;		()	(b)	int &	x ;		(
)								
	(c)	ptr x ;		()	(d)	int *	x ;	()
5	. An a	array is the co	ollection o	of:						
	(a)	different data	a types sca	attered	throug	hout the	memo	ry	()
	(b) 1	the same dat	a type sca	ttered	through	nout the	memor	у	()
	(c) 1	the same dat	a type pla	ced nex	xt to ea	ch other	in mem	nory		(
)		_						
	(d)	different data)	a type pla	ced nex	t to eac	ch other	in mem	ory		(
6	. Con	tinue statem	ent is use	d :						
	(a) 1	to go to the i	next itera	tion in a	a loop					(
)							_	
	(b) 1	to come out o	of the loo	р	¢				()
	(c)	to exit and re	turn to th	e main	tunctio	n c.			()
	(d) 1	to restart iter	ation from	n the b	eginnin	g ot a loc	р		()

7.	7. int testarray [3][2][2] = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12} what values does testarray [2][1][0] in the sample code above contain?											
	(a)	5			()	(b)	7			()
	(c)	9			()	(d)	11			()
8.	Whick	n of the	followir	ng is no	t user –	- define	d types	?				
	(a) s	tructur	es	()		(b)	arrays	i	()	
	(c) e	enumera	ations	()		(d)	all of t	the abo	ve	()
9.	What	is the s	imilarity	/ among	struct	ure. uni	on and	enumer	ation?			
	(a) Al	l of the	m let yo	u defin	e new d	data typ	es;					(
	/b) Al)		dafia							,	,
	(d) Al	l of the	m let yo m let yo	u defini		/aiues;					()
	(C) AI	l of the	m let yo	u defin	e new p	Jointers	,)
10		n of the	followir	u denno	e new s t includ	lod in a	e; structur	o docla	ration?		()
10	(a) st	ruct	TOHOWI	ig is no	((h)	tag na	me		(١
	(a) 30	iuci			()	(6)	tag na	inte		()
	(c) id	entifier	S		()	(d)	all of t	the abo	ve		(
)										
11	Whick	n kevwo	ord is us	ed for s	kinning	nart of	the loo	n?				
		(a)	skip		()		μ.				
		(b)	contin	ue	()						
		(c)	break		()						
		(d)	jump		()						
12	. The v	alue of :	x = 2*3/	4 + 4/8	+ 8 – 2	+ 5/8;						
		(a)	5		()	(b)	6		()	
		(c)	7		()	(d)	8		()	
13	. The d	eclarati	on void	functio	n (int) i	indicate	s functio	on whic	h			
		(a)	return	ı but no	argum	ent		()			
		(b) return nothing but argument ()										
(c) no return no argument ()												
(d) both (i) and (ii). ()												
14	. How i	many tii	mes is a	do – w	hile loo	p guara	nteed t	o loop?				
		(a)	0		1	١		(h)	1		1	١
		(a)	U		()		(u)	T		()

	(c)	indefinitely	()		(d)	unknown	()
15. Which	n one of	the following	is the co	orrect u	sage of	conditio	onal operators	used in	C?
	(a)	a > b ? c = 30	: c = 40;	()	(b)	a>b? c = 30;	()
	(c)	max = a > c?)	a: c : b >	• c? b: c	; () (d)	return (a > b)	? (a: b);	(
16. Which	n one of	the following	is the pr	oper de	eclaratio	on of a p	oointer ?		
(a) * x ;)		()	(b)	int & x	<;		(
(c) ptr	x;	()	(d)	int * x	;	()
17. The k	eyword	used to transfe	er contr	ol from	a func	tion bac	k to the function	on is	
	(a) sv	vitch	()	(b)	goto		()
	(c) re	turn	()	(d)	break		()
18. Which	n of the	following in ch	aracter	– orien	ted con	isole I/O	function?		
	(I) ge	tcher() and pu	tchar()	()	(ii) get	s() and puts()	()
	(iii) so	canf() and prin)	tf()	()	(iv) fge	ets () and fput	s()	(
19. File m	anipula	, tion function i	n C are a	available	e in whi	ich the f	ollowing head	er files?	
	(a) sti	reams.h()			()	(b) stdlib.h()		(
	())			·		()		•
	(c) st	, dio.h()		()	(d) file	es.h()	()
20. What	will be	the output of t	he follo	, wing co	, d? (ass	uming t	hat the union e	exist)	,
	Main()		-		-		·	
	{								
	unio	n student x;							
	x.a = 5	5; x.b = 7;							
	printf	("%d", x.a, x.b	};						
	}								
	(a) 5 a	and 5		()	(b) 7 a	nd 7	()
	(c) 5 a	and 7		()	(d) 7 a	nd 5	()

21. Which of the following is exit – control loop?

	(a) while ()		()	(b) for ()		()				
	(c) do while ()		()	(d) if ()		()				
22	22. Which one of the following gives the memory address of integer variable x ?											
	(a) *x;	()	(b) x;		()					
	(c) & x;)		()	(d) address (x);		(
23	23. The library function used to reverse a string is											
	(a) strstr ()	()	(b) str	rev ()	()					
	(c) revstr ()	()	(d) str	reverse ()		()				
24	24. Which of the following adds one string to the end of another?											
	(a) strcat ()	()	(b) sti	radd ()	()					
	(c) stringadd ()		()	(d) append ()		()				
25	. The unoccupied space betwe	een the	membe	er of a s	tructure is know	wn as						
	(a)slake byte	()	(b) wc	ord boundary	()					
	(c) structure space	()	(d) bit	fields	()					
Part B: Fill up the blanks : 15X1 = 15												
1.	C was developed in the year	·	a	t AT & T	Bell's Laborato	ory .						
2.	A variable name can be max	imum _		charac	ters.							
3. ⊿	The statement	t transfe	ers the o	control	out of the loop	•						
4. 5	is the process	of arra	nging e	ip state dement	ment. is in the list acco	ording t	to their	values				
5. 6.	If the operator p	recedes	a varia	able, it r	eturns the add	ress of	the vari	iable				
	associated with it.			,								
7.	Thefunction	reports	the stat	tus of th	ne file indicated	Ι.						
8.	The function named	rea	ds a cha	aracter	from a file.							
9.	Input/output in C can be ach	ieved u	sing sca	anf() an	id	_functi	ons.					
10	10. && and are binary operators, whereas, ! is a operator.											

- 11. A ______ statement skips the execution of the statements after it and takes the control to the beginning of the loop.
- 12. The ______ keyword is followed by an integer or an expression that evaluates to an integer.
- 13. A function can be called either by value or by _____
- 14. For reading a double type value, we must use the specification ______.
- 15. A ______ is usually used when we wish to store dissimilar data together.

Key Answer

(Part A)

1. (c) 2. (b) 3. (d) 4. (d) 5. (c) 6. (d) 7. (d) 8. (d) 9. (a) 10. (c) 11. (c) 12. (c) 13. (b) 14. (b) 15. (a) 16. (d) 17. (c) 18. (a) 19. (b) 20. (c) 21. (c) 22. (c) 23. (b) 24. (a) 25. (b).

(Part B)

 1. 1972
 2. 31
 3. break
 4. while
 5. sorting
 6. &

 7. feof
 8.getc
 9.printf ()
 10.unary
 11.continue
 12.switch
 13.

 Reference
 14.%lf
 15.structure.

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