## 2017

(5th Semester )

## MATHEMATICS

Paper : MATH-354(A)

## (Operations Research )

## Full Marks : 75

Time : 3 hours

## ( PART : B—DESCRIPTIVE )

(Marks: 50)
The questions are of equal value
Answer five questions, selecting one from each Unit
UNIT-I

1. The manager of an oil refinery must decide on the optimal mix of two possible blending processes of which the inputs and outputs per production run are as follows :

| Process | Input |  | Output |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Crude $A$ | Crude B | Gasoline $X$ | Gasoline $Y$ |
| 1 | 5 | 3 | 5 | 8 |
| 2 | 4 | 5 | 4 | 4 |

The maximum amounts available in crude $A$ and crude $B$ are 200 units and 150 units respectively. Market requirements show that at least 100 units of gasoline $X$ and 80 units of gasoline $Y$ must be produced. The profits per production run from process 1 and process 2 are $₹ 300$ and $₹ 400$ respectively. Formulate an LPP and solve it for maximization of profit.
2. The standard weight of a special purpose brick is 5 kg and it contains two ingredients $A$ and $B$. $A$ costs $₹ 5$ per kg and $B$ costs $₹ 8$ per kg. Strength considerations dictate that the brick contains not more than 4 kg of $A$ and a minimum of 2 kg of $B$. Since the demand for the product is likely to be related to the price of the brick, find the minimum cost of the brick satisfying the above conditions. Use the graphical method.
Unit-II
3. Solve the following LPP using simplex method :

$$
\text { Maximize } Z=5 x_{1}+7 x_{2}
$$

subject to the constraints

$$
\begin{aligned}
x_{1}+x_{2} & \leq 4 \\
3 x_{1}+8 x_{2} & \leq 24 \\
10 x_{1}+7 x_{2} & \leq 35 \\
x_{1}, x_{2} & \geq 0
\end{aligned}
$$

4. Solve the following LPP by Big-M method :

$$
\text { Maximize } Z=x_{1}+x_{2}+x_{3}
$$

subject to the constraints

$$
\begin{aligned}
x_{1}+4 x_{2}+2 x_{3} & \geq 5 \\
3 x_{1}+x_{2}+2 x_{3} & \geq 4 \\
\text { and } x_{1}, x_{2}, x_{3} & \geq 0
\end{aligned}
$$

UnIT-III
5. Use duality to solve the following LPP :

Maximize $Z=3 x_{1}+x_{2}$
subject to the constraints

$$
\begin{aligned}
2 x_{1}+3 x_{2} & \geq 2 \\
x_{1}+x_{2} & \geq 1 \\
x_{1}, x_{2} & \geq 0
\end{aligned}
$$

6. Given $x_{13}=50$ units, $x_{14}=20$ units, $x_{21}=55$ units, $x_{31}=30$ units, $x_{32}=35$ units and $x_{34}=25$ units. With the cost of transportation as

|  | $D_{1}$ | $D_{2}$ | $D_{3}$ | $D_{4}$ | Supply |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $S_{1}$ | 6 | 1 | 9 | 3 | 70 |  |  |  |
| $S_{2}$ | 11 | 5 | 2 | 8 | 55 |  |  |  |
| $S_{3}$ | 10 | 12 | 4 | 7 | 90 |  |  |  |
| Demand | 85 | 35 | 50 | 45 |  |  |  |  |
|  |  |  |  |  |  |  |  |  |

is it an optimum solution to the transportation problem? If not, find the optimum solution.
UnIT—IV
7. Use Gomory's cutting plane method to solve the following LPP :

$$
\text { Maximize } Z=3 x_{1}+4 x_{2}
$$

subject to the constraints

$$
\begin{aligned}
3 x_{1}+2 x_{2} & \leq 8 \\
x_{1}+4 x_{2} & \leq 10 \\
x_{1}, x_{2} & \geq 0 \text { and integers }
\end{aligned}
$$

8. Use the branch and bound technique to solve the following LPP :

$$
\text { Maximize } Z=x_{1}+x_{2}
$$

subject to the constraints

$$
\begin{aligned}
2 x_{1}+5 x_{2} & \leq 16 \\
6 x_{1}+5 x_{2} & \leq 30 \\
x_{1}, x_{2} & \geq 0 \text { and } x_{2} \text { integer }
\end{aligned}
$$

Unit—V
9. Using dominance rule and graphical method, solve the two-person zero-sum game, whose payoff matrix is given below :

Player B
Player $A\left(\begin{array}{cccc}1 & 2 & 3 & -1 \\ 2 & 2 & 1 & 5 \\ 3 & 1 & 0 & -2 \\ 4 & 3 & 2 & 6\end{array}\right)$
10. Reduce the following two-person zero-sum game to an LPP and then solve it using simplex method :

Player B
Player $A\left(\begin{array}{llll}3 & 2 & 4 & 0 \\ 3 & 4 & 2 & 4 \\ 4 & 2 & 4 & 0 \\ 0 & 4 & 0 & 8\end{array}\right)$
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## MATH/V/08a

## 2017 <br> (5th Semester) <br> MATHEMATICS

Paper : MATH-354(A)

## ( Operations Research )

(PART : A—OBJECTIVE )
(Marks: 25 )

SECTION—A
( Marks : 10 )
Each question carries 1 mark

Put a Tick $\nabla$ mark against the correct answer in the box provided:

1. A constraint in an LPP is expressed as
(a) an equation with $=$ sign
(b) an inequality with $\geq$ sign
(c) an inequality with $\leq$ sign
(d) None of the above

## (2)

2. A feasible solution to an LPP should satisfy
(a) all the constraints and $x_{i} \geq 0$
(b) all the constraints and $x_{i} \leq 0$
(c) all the constraints only
(d) None of the above
3. In an LPP with $m$ constraints and $n$ unknowns $(m<n)$, the number of basic variables will be
(a) $n$
(b) $m$
(c) $m+n$
(d) None of the above
4. If there is a negative value in solution values $\left(x_{B}\right)$ of the simplex method, then
(a) the basic solution is optimum
(b) the basic solution is infeasible
(c) the basic solution is unbounded
(d) None of the above

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## ( 3 )

5. The right-hand side constant of a constraint in a primal problem appears in the corresponding dual as
(a) a coefficient in the objective function
(b) a right-hand side constant of a constraint
(c) a value of the objective function
(d) None of the above
6. If there are $n$ workers and $n$ jobs in an assignment problem, there would be
(a) $n$ solutions
(b) $n^{2}$ solutions
(c) $n$ ! solutions
(d) None of the above
7. In cutting plane algorithm, each cut involves the introduction of
(a) an equality constraint
(b) a less than or equal to constraint
(c) an artificial variable
(d) a greater than or equal to constraint
[^0]
## ( 4 )

8. Branch and bound method divides the feasible solution space into smaller parts by
(a) enumerating
(b) bounding
(c) branching
(d) None of the above
9. A game is said to be strictly determinable, if
(a) minimax value is greater than maximin value
(b) minimax value is equal to maximin value
(c) minimax value is less then maximin value
(d) None of the above
10. The size of a payoff matrix of a game can be reduced by using the principle of
(a) dominance
(b) rotation reduction
(c) game inversion
(d) None of the above

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## ( 5 )

## SECTION-B

(Marks : 15 )

## Each question carries 3 marks

1. Solve the following LPP by graphical method :

Maximize $Z=2 x_{1}+x_{2}$
subject to

$$
\begin{aligned}
3 x_{1}+5 x_{2} & \leq 15 \\
3 x_{1}-4 x_{2} & \leq 12 \\
x_{1}, x_{2} & \geq 0
\end{aligned}
$$

## ( 6 )

2. Using simplex method, solve the following simultaneous equations :

$$
\begin{aligned}
5 x+y & =11 \\
2 x-3 y & =1
\end{aligned}
$$

## ( 7 )

3. Find the optimal assignment to find the minimum cost for the following problem :


## ( 8 )

4. Use cutting plane method to solve the following integer linear programming problem :

Maximize $Z=2 x_{1}+x_{2}$
subject to

$$
\begin{aligned}
-x_{1}+8 x_{2} & \leq 24 \\
x_{1} & \leq 4 \\
x_{1}, x_{2} & \geq 0 \text { and integers }
\end{aligned}
$$

## ( 9 )

5. For what value of $\lambda$, the game with the following payoff matrix is strictly determinable?

| $B$ |  |  |
| :---: | :---: | :---: |
| $A$ |  |  |
| $\lambda$ 6 2 <br> -1 $\lambda$ 0 <br> 2 4 $\lambda$ |  |  |


[^0]:    MATH/V/08a/225

